Abteilung für Mathematische Logik

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Infinite Games

Sommersemester 2019 Exercise sheet 5, 27.06.2019

Consider the Banach-Mazur game $G^*(A)$ (on 2^{ω}) for a given flip set $F \subseteq 2^{\omega}$.

- 1. Show that if I has a ws in $G^*(F)$, then I also has a ws in $G^*(2^{\omega} \setminus F)$ (the same for player II).
- 2. Show that if II has a ws in $G^*(F)$, then I has a ws in $G^*(2^{\omega} \setminus F)$.
- 3. Show that if I has a ws in $G^*(F)$, then II has a ws in $G^*(2^{\omega} \setminus F)$.
- 4. Show that if there exists an ultrafiler on ω , then there exists a flip set.