**Abteilung für Mathematische Logik** Dr. Giorgio Laguzzi Christian Bräuninger Infinitary Combinatorics Wintersemester 2019/20

## Übungsblatt 7

Abgabe am 17.12.2019 vor der Vorlesung

**Exercise 1. (4 points)** Let  $\kappa > \omega$  be a regular cardinal. Show that a set  $X \subseteq \kappa$  is closed if and only if it closed with respect to the order topology on  $\kappa$ .

**Exercise 2.** (4 points) Let  $\kappa > \omega$  be a regular cardinal and  $X \subseteq \kappa$  consist of only successor ordinals.

- a) Can X be club?
- b) Can X be a stationary set?

Now consider  $X' \subseteq \kappa$  to be a subset that only consists of limits of successor ordinals.

c) Can X' be a stationary set?

**Exercise 3.** (4 points) Let A be a set of infinite cardinals such that for all regular  $\lambda$  the set  $A \cap \lambda$  is not stationary in  $\lambda$ . Show that there is an injective function g on A such that  $\forall \alpha \in A(g(\alpha) < \alpha)$ .