

R. Schneider, *Convex Bodies – The Brunn–Minkowski Theory*. Second expanded edition. Encyclopedia of Mathematics and Its Applications **151**, Cambridge University Press, Cambridge, xxii+736 pp, 2014.

**ERRATA** (last update: October 1, 2023)

p. 57, line 14: Replace ‘max’ by ‘sup’.

p. 82, Theorem 2.2.11(b): As Daniel Hug pointed out, it must still be proved that  $N(K, x) + N(L, x)$  is closed. To prove this, we may assume that  $x \in \text{bd } K \cap \text{bd } L$  and  $\text{aff}(K \cup L) = \mathbb{R}^n$ . Let  $a_i \in N(K, x)$ ,  $b_i \in N(L, x)$  such that  $a_i + b_i \rightarrow c$  as  $i \rightarrow \infty$ . If  $(a_i)$  is bounded, then also  $(b_i)$  is bounded, and both sequences have convergent subsequences, which gives  $c \in N(K, x) + N(L, x)$ . Suppose  $(a_i)$ ,  $(b_i)$  are both unbounded. Then we can assume that  $a_i, b_i \neq 0$  and hence  $a_i = \lambda_i u_i$ ,  $b_i = \mu_i v_i$  with unit vectors  $u_i, v_i$  and  $\lambda_i, \mu_i \rightarrow \infty$ . A subsequence of  $(u_i)$  converges to some  $u \in N(K, x)$ , and a subsequence of  $(v_i)$  converges to some  $v \in N(L, x)$ . The convergence  $\lambda_i u_i + \mu_i v_i \rightarrow c$  implies that  $u = -v$ . But then  $K$  and  $L$  are separated by the hyperplane through  $x$  orthogonal to  $u, v$ , which contradicts Theorem 1.3.8.

p. 136, lines 10–11: The assertion saying that  $P + \varepsilon B^n \in \mathcal{K}_r^n \setminus \mathcal{A}_k$ , is not correct. Instead, the proof of Theorem 2.7.2 should use the original argument of Zamfirescu [2038].

p. 156, Proof of Theorem 3.2.1: Without loss of generality, assume  $\dim K = n$ .

p. 219, line after (4.33): Replace “Theorem 3.2.3” by “Theorem 3.2.22”.

p. 286, equation (5.33): The factor  $\frac{1}{n}$  is missing on the right side.

p. 294, equation (5.43): The factor  $\frac{1}{n}$  is missing on the right side.

p. 303, line -8: Replace  $E$  by  $E^\perp$ .

p. 317, line 5: Replace  $\Psi_{r-1}(e_{i_1}, \dots, \check{e}_{i_k}, \dots, e_{i_r})$  by  $\Psi_{r-1}(K)(e_{i_1}, \dots, \check{e}_{i_k}, \dots, e_{i_r})$ .

p. 318: In lines 8, 9, 10,  $\phi_j$  must be replaced by  $A_j$ .

p. 319, line -13: Replace ‘Note 7’ by ‘Note 9’.

p. 344, line -2: Replace  $\varphi$  by  $\bar{\varphi}$ .

p. 345, line -6: Replace  $\varphi$  by  $\bar{\varphi}$ .

p. 346, line 4: Replace ‘Theorem 6.3.4’ by ‘Theorem 6.3.1’.

p. 351, line 13: Replace  $\mathbb{R}^n$  by  $\mathbb{R}$ .

p. 357: In lines 4, -9, -3,

$$\int_{\mathbb{S}^{n-1}} \text{ must be replaced by } \int_{\mathbb{S}^{n-1}} \cdots \int_{\mathbb{S}^{n-1}} (m \text{ integrals}).$$

p. 401, lines -10, -11: Replace ‘Minkowski’s inequality (7.18)’ by ‘the Aleksandrov–Fenchel inequality (7.54)’.

p. 459, line -11: Replace ‘Theorem 9.1.4’ by ‘Theorem 9.2.1’.

p. 501, line -2: Replace  $K$  by  $K_j$ .

p. 539, after Theorem 10.3.5: The reference to Pfiefer [1532] is misleading, since Pfiefer considers different ranges of the parameters.

p. 569, l. 11: Reference [1511] must be replaced by the following one, which is missing in the bibliography:

Paouris, G., Pivovarov, P., A probabilistic take on isoperimetric-type inequalities. *Adv. Math.* **230** (2012), 1402–1422.

p. 575, line -9: The assumption  $\phi(0) = 0$  must be added.

p. 578, first line of Note 7: Replace [1698] by [1697].

p. 646, reference [415]: Replace (2911) by (2011).

p. 675, reference [1119]: Insert (1981).

p. 680, reference [1260]: Replace (1932) by (1935).

p. 698, reference [1699]: Replace (19983) by (1983).

p. 710, reference [1992]: Replace (2001) by (1901).

### Updates of references

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